

# Mean field simulation for Monte Carlo integration

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**Lectures, INLN CNRS & Nice Sophia Antipolis Univ. 2012**

## Some hyper-refs

- ▶ **Mean field simulation for Monte Carlo integration.** Chapman & Hall - Maths & Stats [600p.] (May 2013).
- ▶ **Feynman-Kac formulae,** Genealogical & Interacting Particle Systems with appl., Springer [573p.] (2004)
- ▶ **More references on the website**<http://www.math.u-bordeaux1.fr/~delmoral/index.html> [+ Links]

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